

$$5a)i) (3x+5)^2 - 2 = 9x^2 + 30x + 25 - 2 = 9x^2 + 30x + 23$$

$$ii) 3(x^2 - 2) + 5 = 3x^2 - 6 + 5 = 3x^2 - 1$$

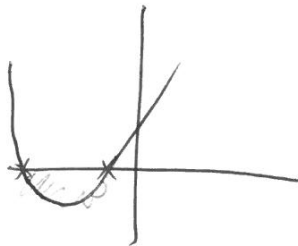
$$b) 9x^2 + 30x + 23 < 3x^2 - 1$$

$$6x^2 + 30x + 24 < 0$$

$$6(x^2 + 5x + 4) < 0$$

$$(x+4)(x+1)$$

$$x = -4 \quad x = -1$$



$$\underline{\underline{-4 < x < -1}}$$

Question			Generic scheme	Illustrative scheme	Max mark
5.	(a)	(i)	$\bullet^1$ interpret notation $\bullet^2$ state expression for $f(g(x))$	$\bullet^1 f(3x+5)$ or $(g(x))^2 - 2$ $\bullet^2 (3x+5)^2 - 2$	2
		(ii)	$\bullet^3$ state expression for $g(f(x))$	$\bullet^3 3(x^2 - 2) + 5$	1
Notes:					
1. For $f(g(x)) = (3x+5)^2 - 2$ without working, award both $\bullet^1$ and $\bullet^2$.					
Commonly Observed Responses:					
Candidate A (a)(i) $f(g(x)) = 3(x^2 - 2) + 5$ $\bullet^1$ ✗ $\bullet^2$ ✓ 1 (a)(ii) $g(f(x)) = (3x+5)^2 - 2$ $\bullet^3$ ✓ 1					

Question			Generic scheme	Illustrative scheme	Max mark
5.	(b)		•⁴ interpret information and expand •⁵ express inequality in standard quadratic form •⁶ determine zeros of quadratic equation •⁷ state range with justification	•⁴ $9x^2 + 30x + 25 - 2 < 3x^2 - 6 + 5$ •⁵ $6x^2 + 30x + 24 < 0$ •⁶ $-4, -1$ •⁷ $-4 < x < -1$ with eg sketch or table of signs	4
Notes:					
2. Candidates who do not work with an inequation from the outset lose •⁴, •⁵ and •⁷. However, •⁶ is still available. See Candidate D. 3. Accept the appearance of $-4, -1$ within inequalities for •⁶. 4. At •⁷ accept "$x > -4$ and $x < -1$" or "$x > -4, x < -1$" together with the required justification.					
Commonly Observed Responses:					
Candidate B			Candidate C		
$9x^2 + 30x + 25 - 2 < 3x^2 - 6 + 5$			$9x^2 + 30x + 25 - 2 < 3x^2 - 6 + 5$	• ⁴ ✓	
$6x^2 + 30x + 24 < 0$			$6x^2 + 30x + 24 = 0$	• ⁵ ✗	
$6x^2 + 30x + 24 = 0$			$x = -1, x = -4$	• ⁶ ✓	
$x = -1, x = -4$			$-4 < x < -1$ with sketch	• ⁷ ✗	
$-4 < x < -1$ with sketch					
Candidate D					
$9x^2 + 30x + 25 - 2 = 3x^2 - 6 + 5$				• ⁴ ✗	
$6x^2 + 30x + 24 = 0$				• ⁵ ✗	
$x = -1, x = -4$				• ⁶ ✓	
For $f(g(x)) < g(f(x))$					
$-4 < x < -1$ with sketch				• ⁷ ✗	